

ECE 264 Spring 2023
***Advanced* C Programming**

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Homework 11-12

Shuffle Cards



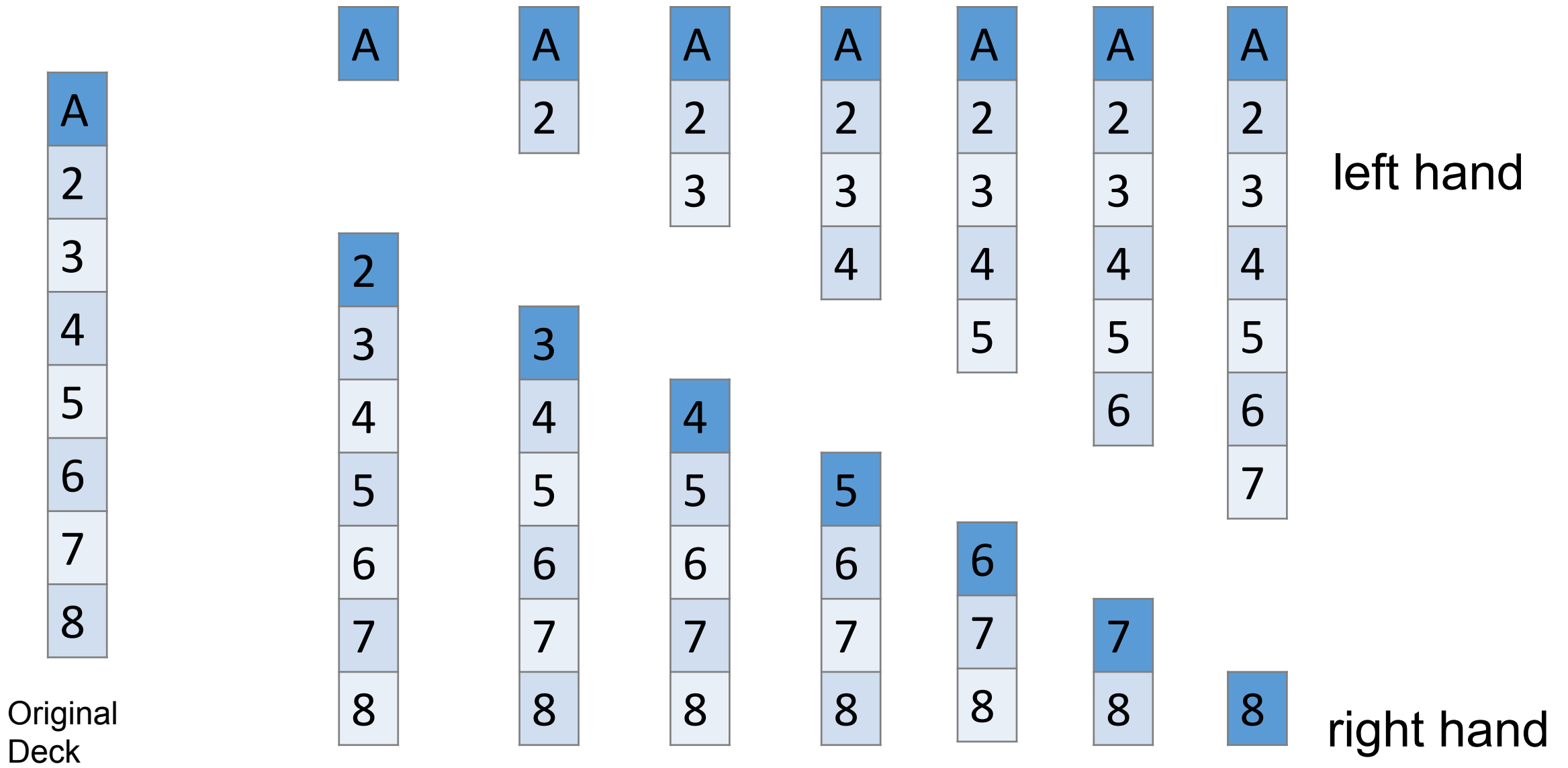
Riffle Shuffling

- Many card games need to shuffle so that players do not know which card may appear next.
- Riffle shuffling is a popular method for shuffling
 1. divide a deck of cards into two parts
 2. hold the parts by right and left hands
 3. interleave the cards



Homework 11-12

- Homework 11: Shuffle Once
- Homework 12: Shuffle Multiple Times
- The homework considers all possible scenarios under these restrictions:
 - Each (of the two) part has at least one card
 - If a card is above another card in one part, the order must be preserved in the interleave result

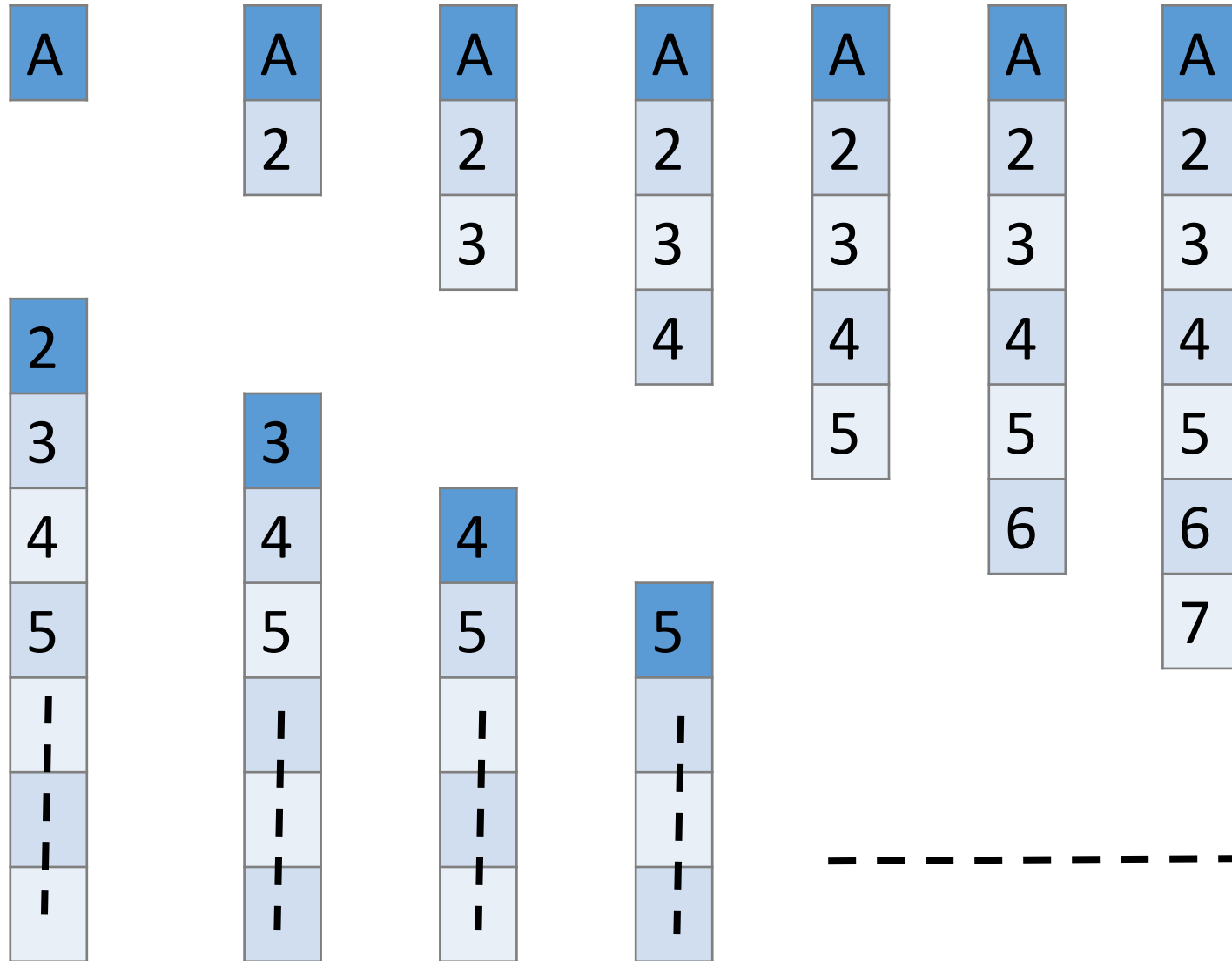


Different ways to divide the original deck into two parts



Original

Deck n cards



Different ways to divide the original deck into two parts

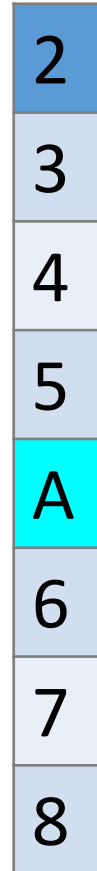
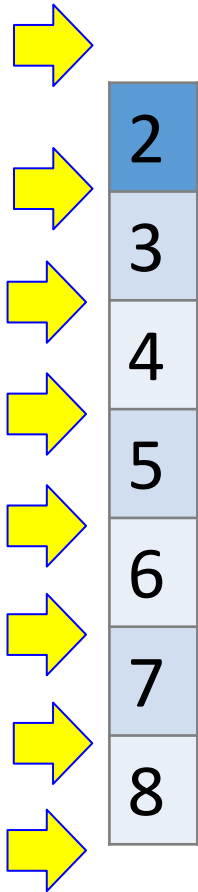
The first part has $1, 2, 3, \dots, n - 1$ cards

$n - 1$ ways to divide the cards

A

Where can A be placed?

The order 2, 3, 4, 5, 6, 7, 8 **will not change**



Above 2

Between
2 and 3

Between
3 and 4

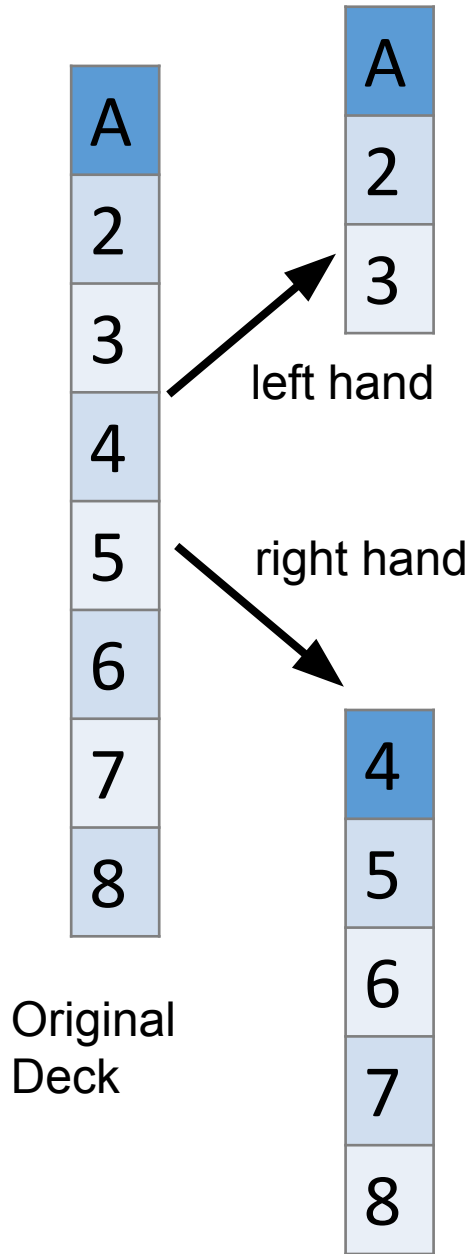
Between
4 and 5

Between
5 and 6

Between
6 and 7

Between
7 and 8

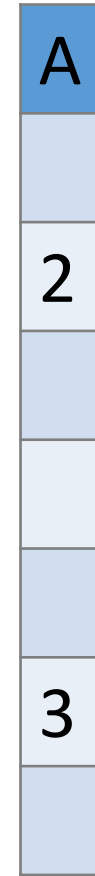
Below 8

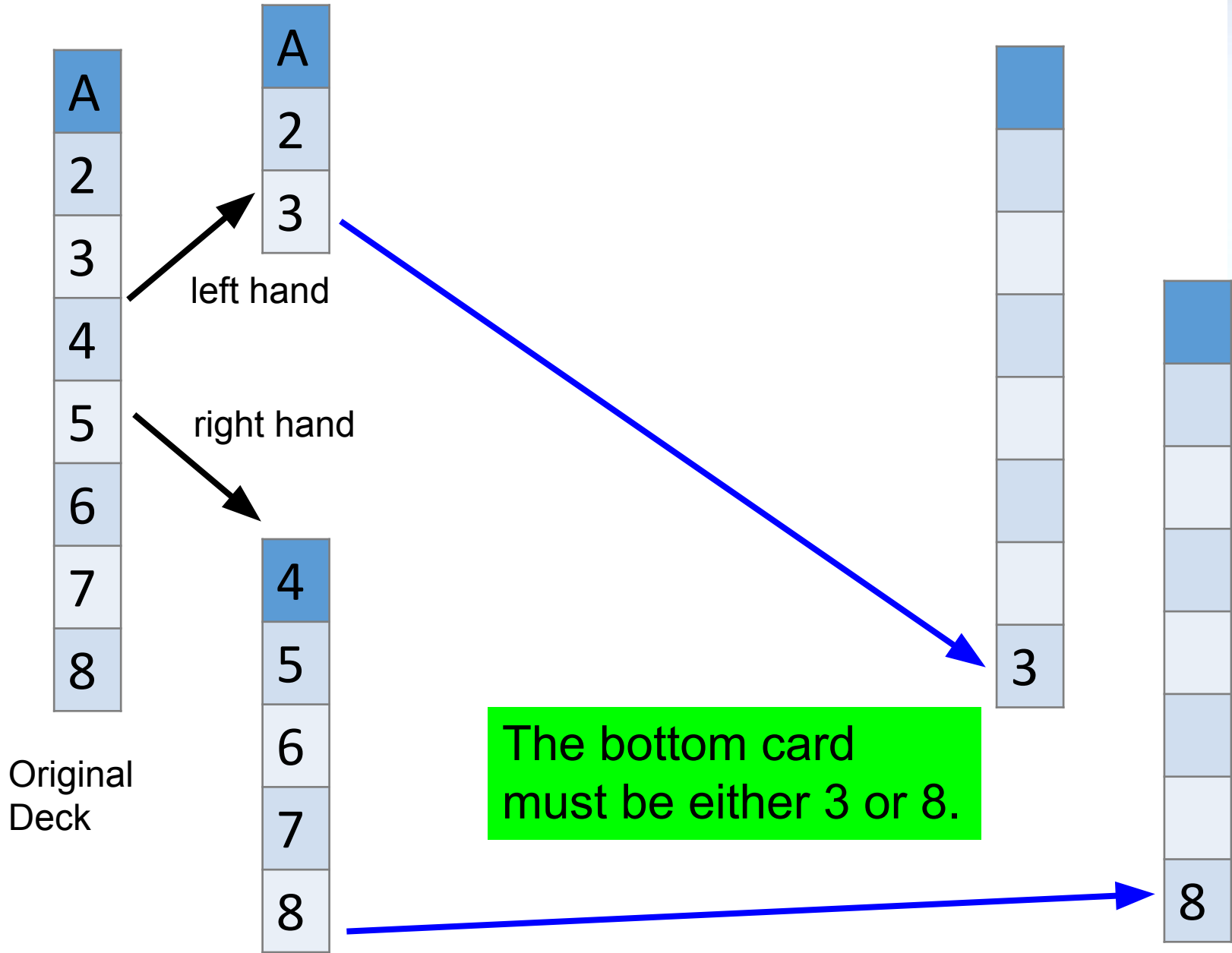


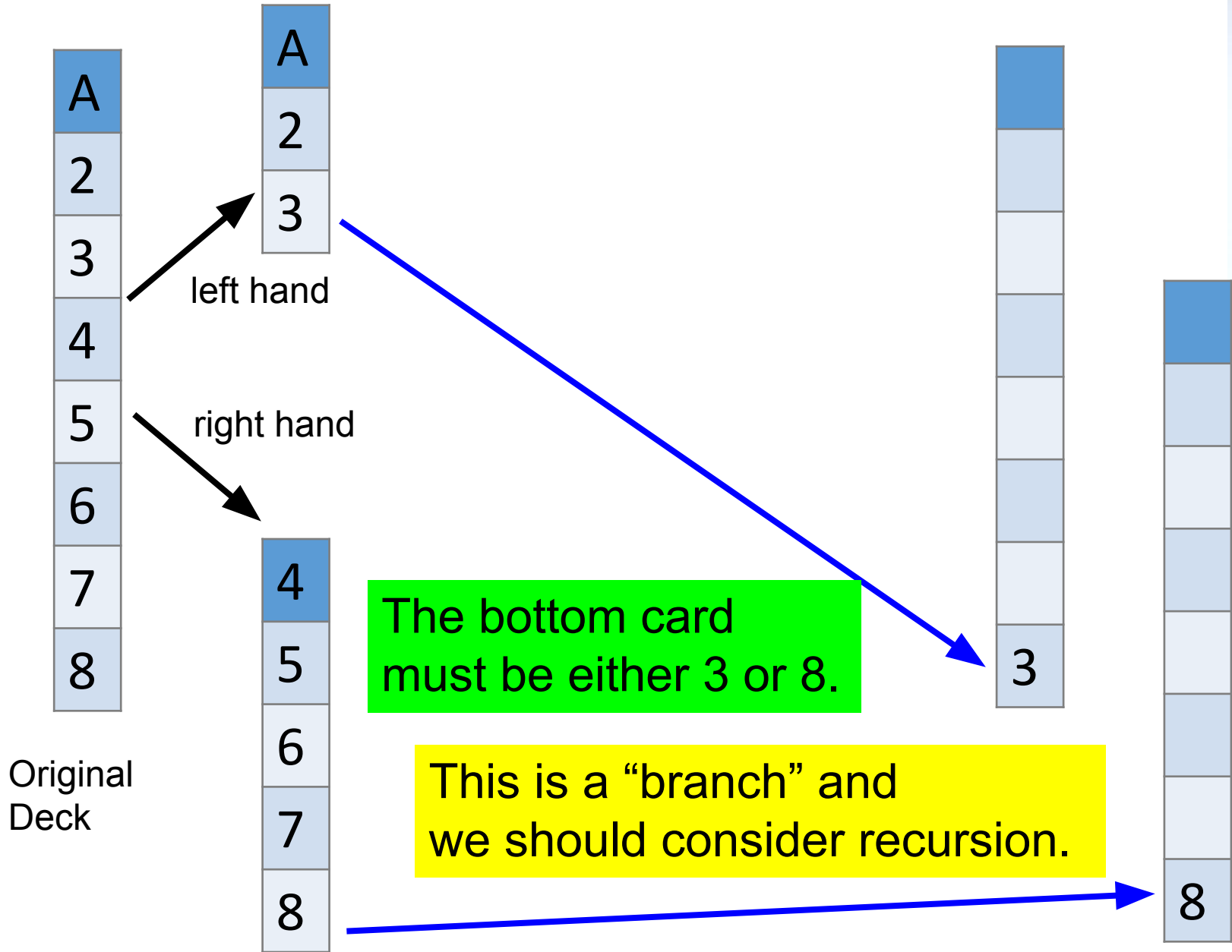
mix the cards →

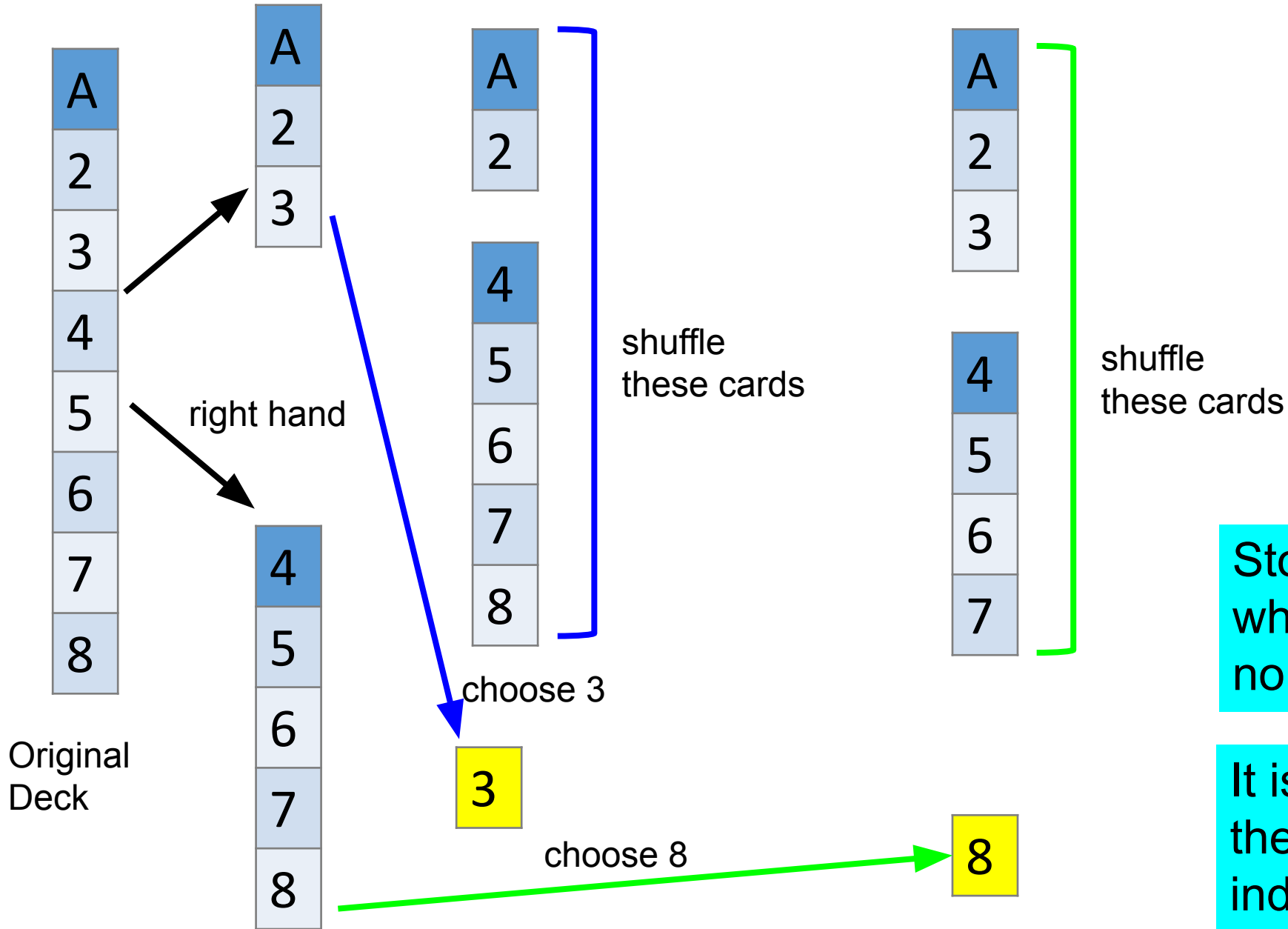
The order A, 2, 3 **will not change**

The order 4, 5, 6, 7, 8 **will not change**









Stop condition:
when one hand has
no card left

It is easier to start from
the bottom. The top's
index must be zero

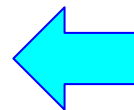
Homework 13-14

Arithmetic Operations

HW13 and HW 14

- Use linked list to handle arithmetic expressions
- Understand infix and postfix expressions.
- Convert infix to postfix expressions.
- Use linked list as stack

```
Node * List_insert(Node * h, int v)
{
    Node * p = Node_construct(v);
    p -> next = h;
    return p;
}
```



The new node (p) is
in front of the previous node

Infix and postfix expressions (for binary operations)

- Unary operations: an operator (such as negation) needs only one operand. Binary operations: an operator (such as +, -, *) needs two operands
- infix: operand operation operand, e.g. $4 + 9$
- postfix: operand operand operation, e.g. $4 9 +$
- postfix: easier for computers, no need of parenthesis
 - $3 5 * 6 +$ (postfix) means $3 * 5 + 6 = 15 + 6 = 21$
 - $3 5 + 6 *$ means $(3 + 5) * 6 = 8 * 6 = 48$
 - $3 5 6 + *$ means $3 * (5 + 6) = 3 * 11 = 33$

C Operator Precedence

The following table lists the precedence and associativity of C operators. Operators are listed top to bottom, in descending precedence.

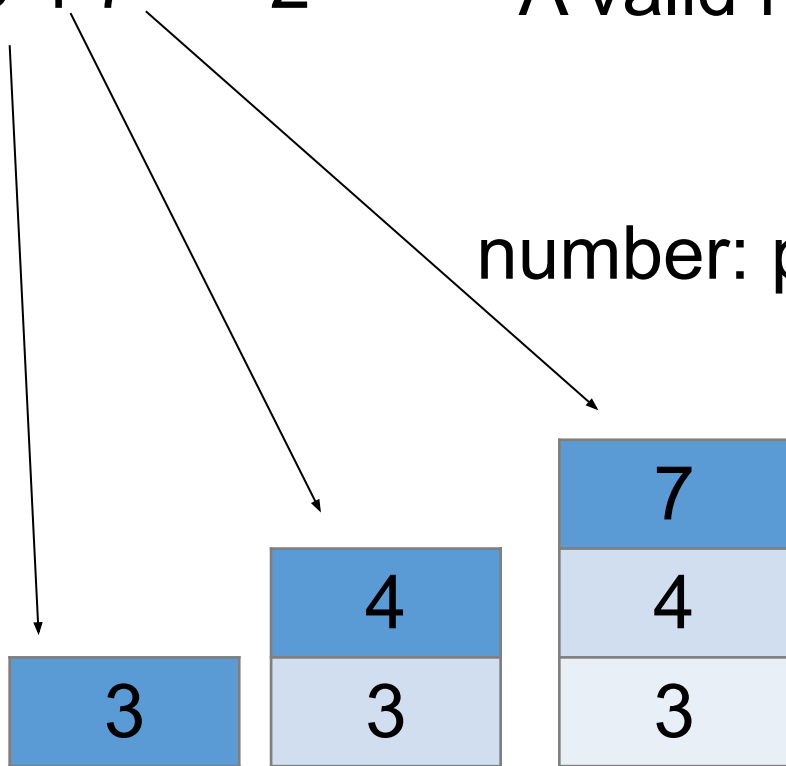
Precedence	Operator	Description	Associativity	
1	++ --	Suffix/postfix increment and decrement	Left-to-right	
	()	Function call		
	[]	Array subscripting		
	.	Structure and union member access		
	->	Structure and union member access through pointer		
	(type){ list }	Compound literal(c99)		
2	++ --	Prefix increment and decrement ^[note 1]	Right-to-left	
	+ -	Unary plus and minus		
	! ~	Logical NOT and bitwise NOT		
	(type)	Cast		
	*	Indirection (dereference)		
	&	Address-of		
	sizeof	Size-of ^[note 2]		
_Alignof	Alignment requirement(c11)			
3	* / %	Multiplication, division, and remainder	Left-to-right	
4	+ -	Addition and subtraction		
5	<< >>	Bitwise left shift and right shift		
6	< <=	For relational operators < and ≤ respectively		
	> >=	For relational operators > and ≥ respectively		
7	== !=	For relational = and ≠ respectively		
8	&	Bitwise AND		
9	^	Bitwise XOR (exclusive or)		
10		Bitwise OR (inclusive or)		
11	&&	Logical AND		
12		Logical OR		
13	?:	Ternary conditional ^[note 3]		Right-to-left
14 ^[note 4]	=	Simple assignment		
	+= -=	Assignment by sum and difference		
	*= /= %=	Assignment by product, quotient, and remainder		
	<<= >>=	Assignment by bitwise left shift and right shift		
	&= ^= =	Assignment by bitwise AND, XOR, and OR		
15	,	Comma	Left-to-right	

Evaluate Postfix using a stack

3 4 7 * + 2 -

A valid must start with a number

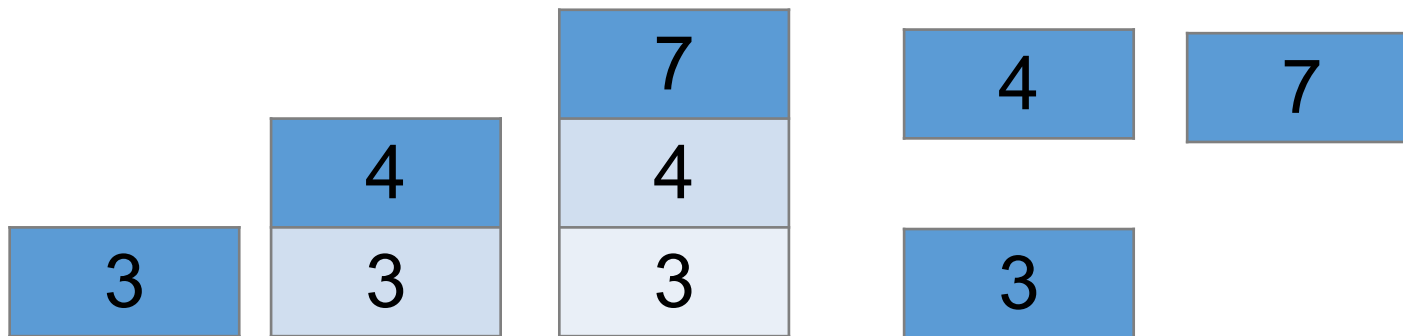
number: push to stack



Evaluate Postfix using a stack

3 4 7 * + 2 -

an operator
pop two numbers

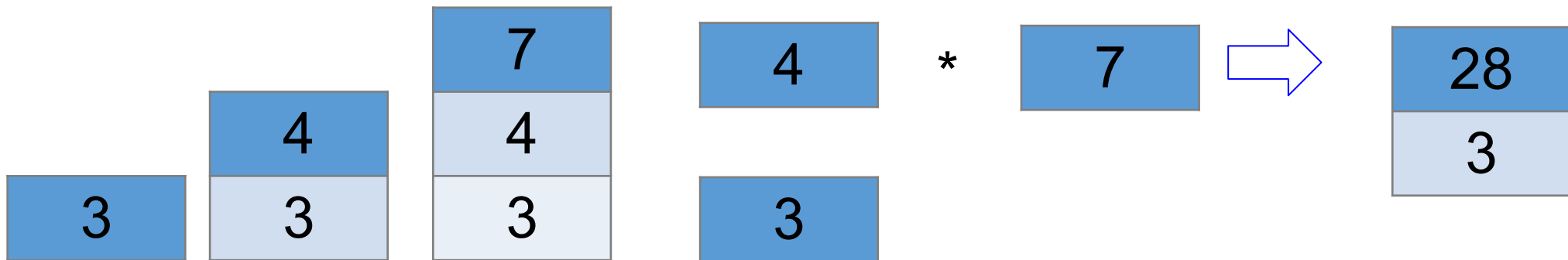


Evaluate Postfix using a stack

3 4 7 * + 2 -

an operator
pop two numbers

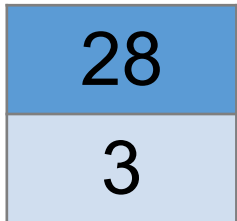
push to stack



Evaluate Postfix using a stack

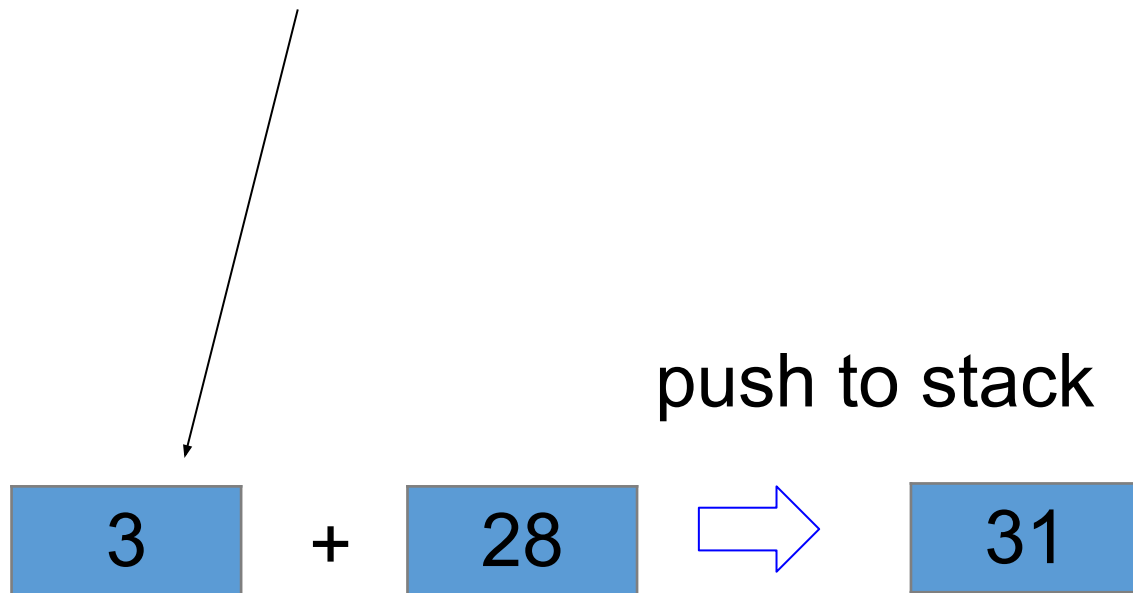
3 4 7 * + 2 -

an operator
pop two numbers



Evaluate Postfix using a stack

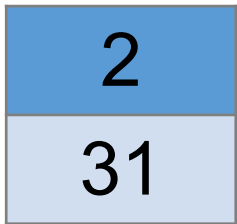
3 4 7 * + 2 -



Evaluate Postfix using a stack

3 4 7 * + 2 -

number: push to stack



Evaluate Postfix using a stack

3 4 7 * + 2 -

an operator
pop two numbers
be careful of the order



An operation is **commutative**
if the order can be changed

$$a + b = b + a$$

$$a * b = b * a$$

$a - b$ is different from $b - a$

Evaluate Postfix using a stack

3 4 7 * + 2 -

an operator
pop two numbers
be careful of the order

push to stack



Evaluate Postfix using a stack

3 4 7 * + 2 -

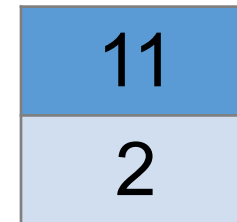
nothing left in the input
final result: 29



29

Handle Errors

- The stack must have two (or more) numbers when an operator is seen. $7 +$ is invalid. $*$ (no number) is invalid
- After finishing the number, there should be exactly one number left. $2 8 3 +$ is invalid because the result is



Convert infix to postfix

Convert $6 * 4 + 3$

Stack: first-in, last-out
Queue: first-in, first-out



operator
(stack)



output
(queue)

Convert infix to postfix

Convert $6 * 4 + 3$

a number, move to output



operator
(stack)



6
output
(queue)

Convert infix to postfix

Convert $6 * 4 + 3$

an operator, move to operator stack

*

operator

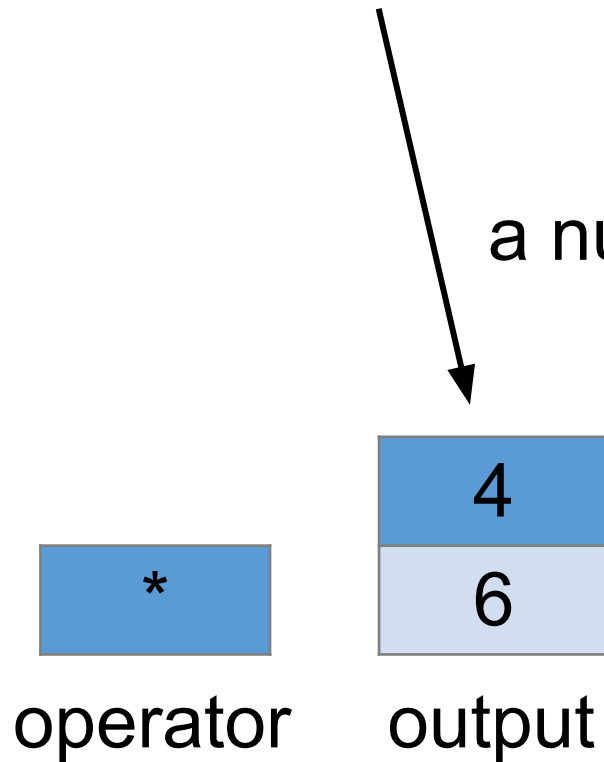
6

output

Convert infix to postfix

Convert $6 * 4 + 3$

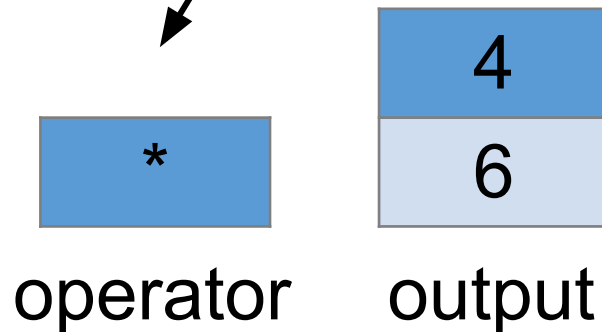
a number, move to output



Convert infix to postfix

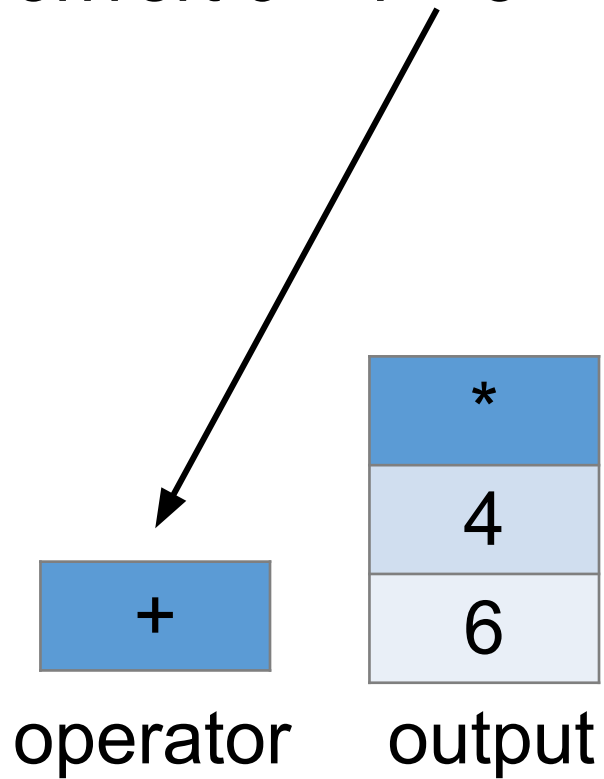
Convert $6 * 4 + 3$

an operator, compare its precedence with $*$
 $*$ has higher precedence, pop and move to output
push + to operator



Convert infix to postfix

Convert $6 * 4 + 3$



Convert infix to postfix

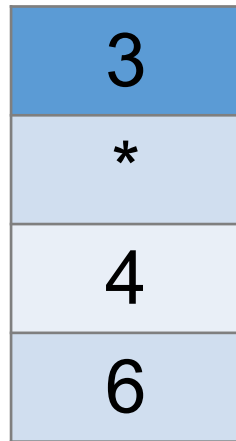
Convert $6 * 4 + 3$



a number, move to output

+

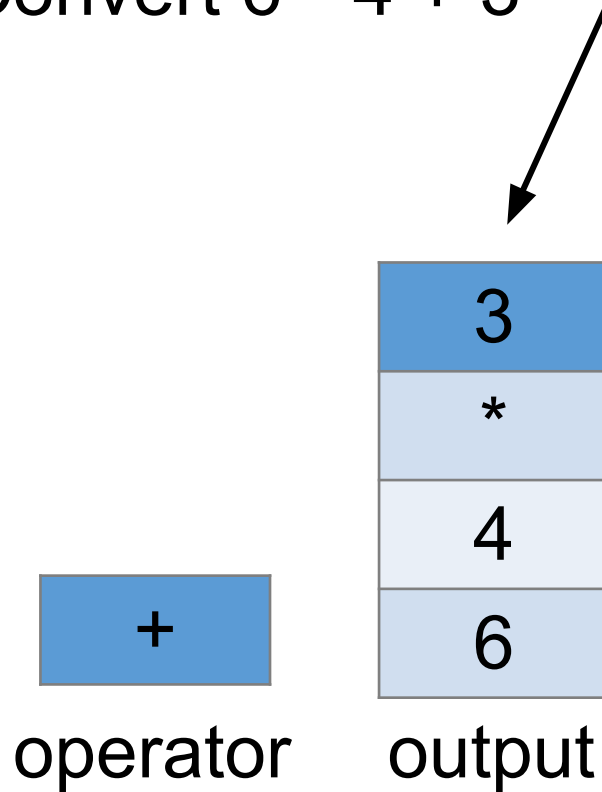
operator



output

Convert infix to postfix

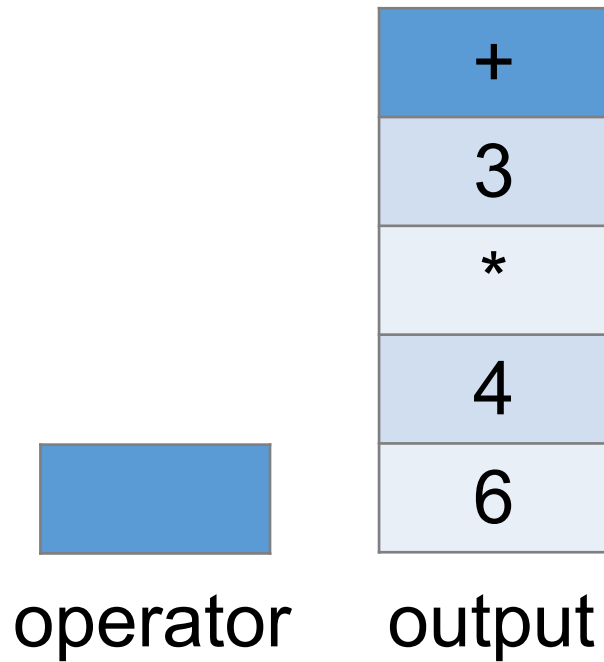
Convert $6 * 4 + 3$



no more input
pop operator
push to output

Convert infix to postfix

Convert $6 * 4 + 3$



postfix: $6 4 * 3 +$

Convert infix to postfix

Convert $6 + 4 * 3$ (different from the previous: **+ * exchanged**)



operator
(stack)



output
(queue)

Convert infix to postfix

Convert $6 + 4 * 3$

a number, move to output



operator



output

Convert infix to postfix

Convert $6 + 4 * 3$

an operator, move to operator stack

+

operator

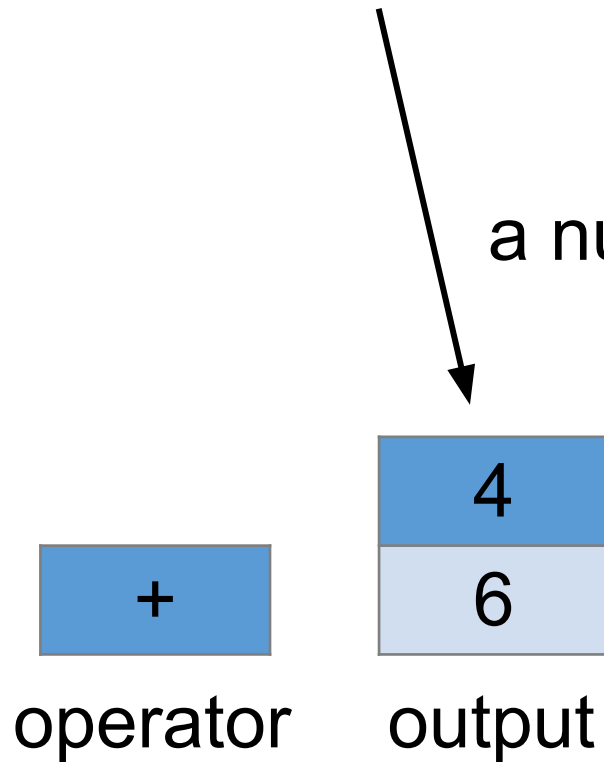
6

output

Convert infix to postfix

Convert $6 + 4 * 3$

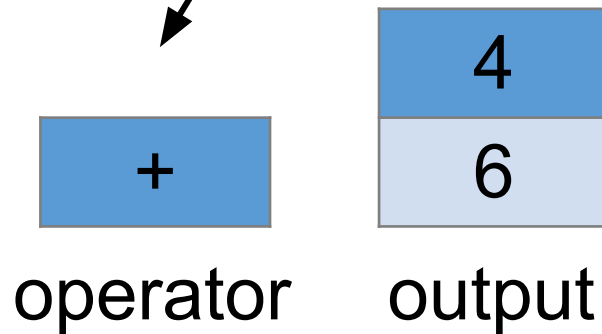
a number, move to output



Convert infix to postfix

Convert $6 + 4 * 3$

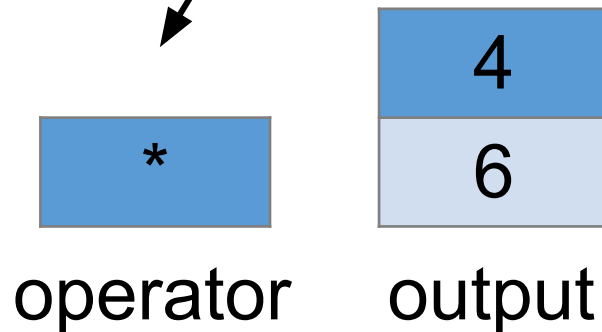
an operator, compare its precedence with +
* has higher precedence, **push * to operator**



(Review) Convert infix to postfix

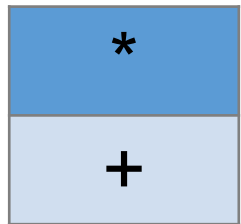
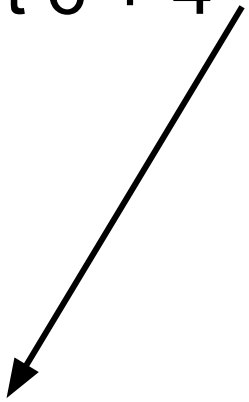
Convert $6 * 4 + 3$

an operator, compare its precedence with $*$
 $*$ has higher precedence, pop and move to output
push + to operator

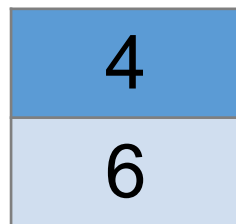


Convert infix to postfix

Convert $6 + 4 * 3$



operator

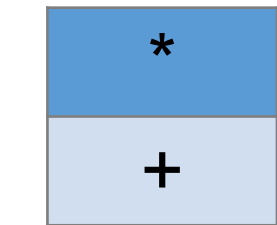


output

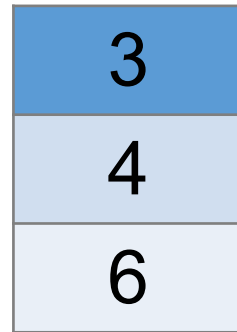
Convert infix to postfix

Convert $6 + 4 * 3$

a number, move to output



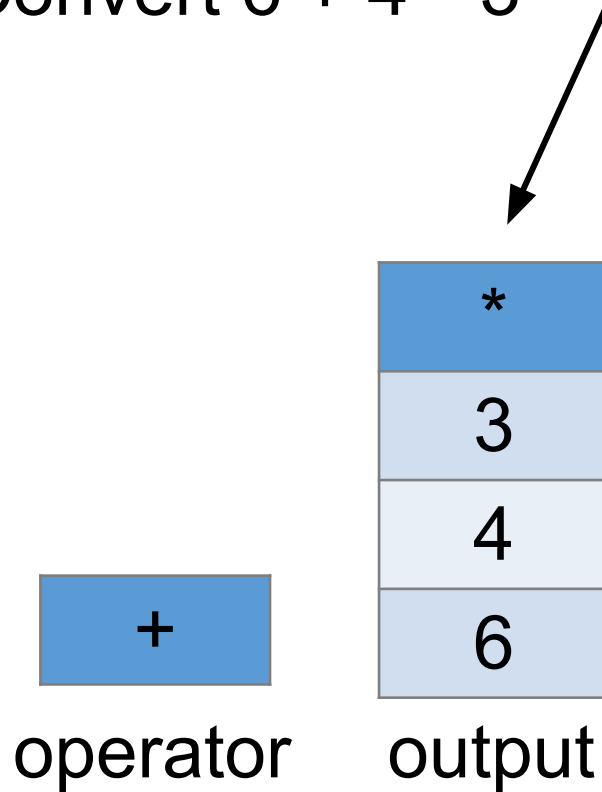
operator



output

Convert infix to postfix

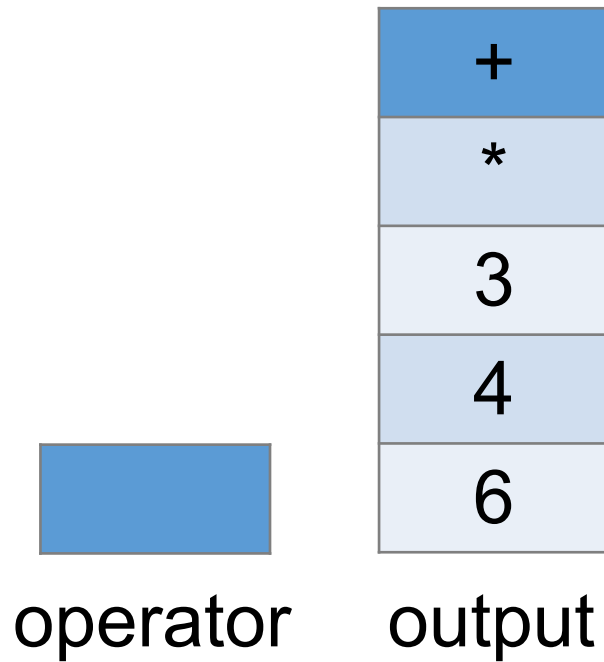
Convert $6 + 4 * 3$



no more input
pop operator
push to output

Convert infix to postfix

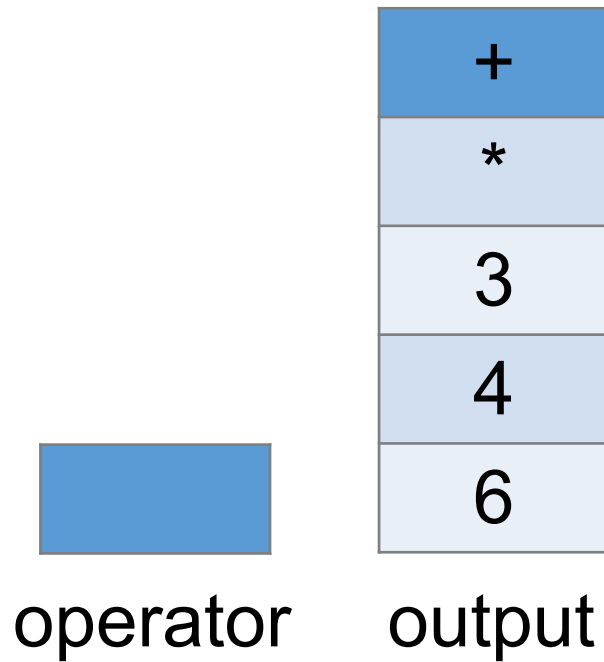
Convert $6 + 4 * 3$



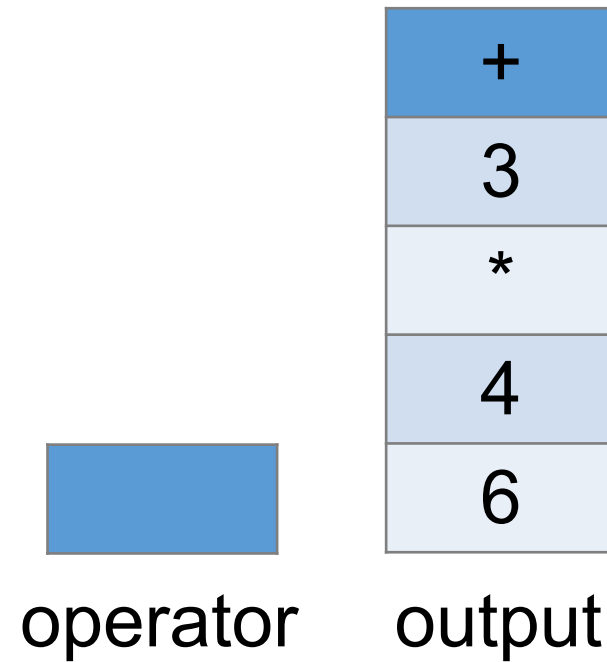
Postfix: $6\ 4\ 3\ *\ +$

Convert infix to postfix

Convert $6 + 4 * 3$



Convert $6 * 4 + 3$



Convert infix to postfix

Convert $6 * (4 + 3)$



operator



output

Convert infix to postfix

Convert $6 * (4 + 3)$

a number, move to output



operator



output

Convert infix to postfix

Convert $6 * (4 + 3)$

an operator, move to operator stack

*

operator

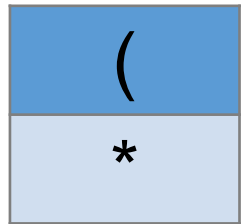
6

output

Convert infix to postfix

Convert $6 * (4 + 3)$

open parenthesis, move to operator stack



operator

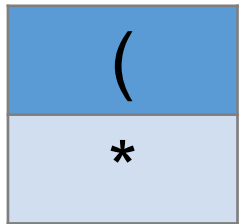


output

Convert infix to postfix

Convert $6 * (4 + 3)$

a number, move to output



operator

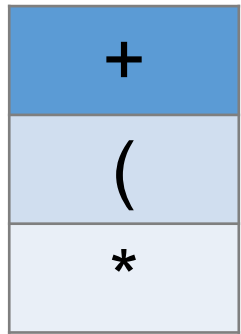


output

Convert infix to postfix

Convert $6 * (4 + 3)$

an operator, move to operator stack



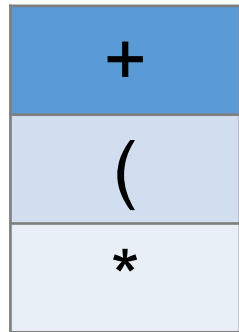
operator

output

Convert infix to postfix

Convert $6 * (4 + 3)$

a number, move to output



operator

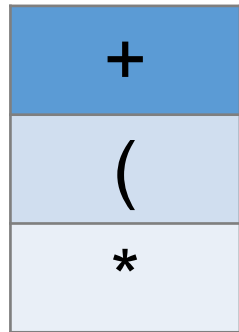


output

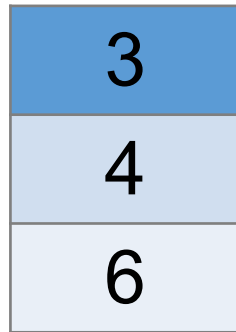
Convert infix to postfix

Convert $6 * (4 + 3)$

close parenthesis
pop until open parenthesis



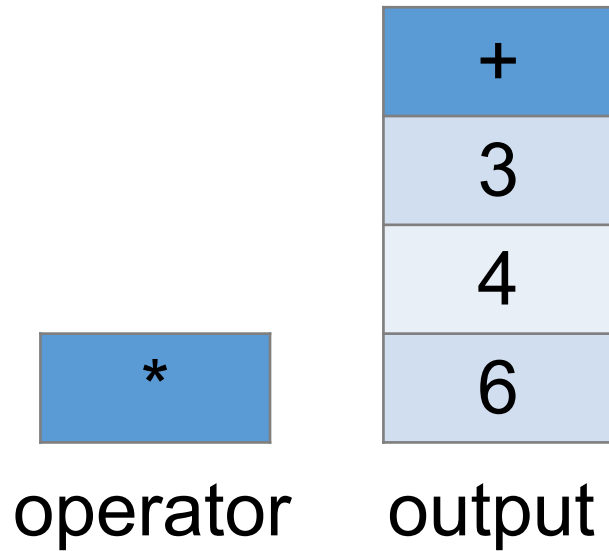
operator



output

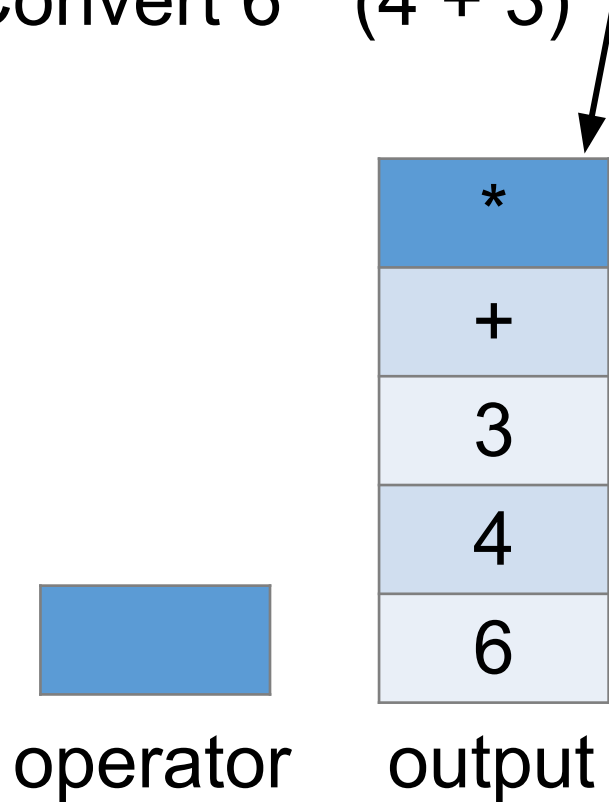
Convert infix to postfix

Convert $6 * (4 + 3)$



Convert infix to postfix

Convert $6 * (4 + 3)$



no more input
pop operator
push to output

postfix: 6 4 3 + *